

Chapter 6 Section 4

Solving Absolute-
Value Equations

6.4) Absolute Value Review

- Absolute Value equations have two answers

Examples:

$$|5| = 5 \quad |9| = 9 \quad |1| = 1$$

$$|-5| = 5 \quad |-9| = 9 \quad |-1| = 1$$

Solving Absolute Value Equations

- o Steps:
 - o Isolate the Absolute Value
 - o Set equation equal to positive and negative → *inside*
 - o Solve for the Variable
 - o CHECK YOUR WORK!

Examples:

- 1. $|x| = 6$

$$x = 6, -6$$

- 2. $|x| = 14$

$$x = 14, -14$$

Examples:

3. $|x| + \cancel{3} = 22$

~~$+3$~~ ~~-3~~

$|x| = 19$

$x = 19, -19$

4. $|x| - \cancel{4} = 12$

~~-4~~ ~~$+4$~~

$|x| = 16$

$x = 16, -16$

Examples

$$5. |x| - 7 = 2$$

~~+7 +7~~

$$|x| = 9$$
$$\boxed{x = 9, -9}$$

$$6. |x| + 6 = 8$$

~~-6 -6~~

$$|x| = 2$$
$$\boxed{x = 2, -2}$$

Examples

$$7.) |x + 1| = 2$$

$$\begin{array}{l|l} x+1=2 & x+1=-2 \\ -1 -1 & -1 -1 \\ \hline x=1 & x=-3 \end{array}$$

$$8.) |x - 3| = 7$$

$$\begin{array}{l|l} x-3=7 & x-3=-7 \\ +3 +3 & +3 +3 \\ \hline x=10 & x=-4 \end{array}$$

Examples

$$9.) |2x + 1| = 9$$

$$\begin{array}{l|l} 2x+1=9 & 2x+1=-9 \\ \hline -1 & -1 \\ 2x=8 & 2x=-10 \\ \hline \cancel{2}x=4 & \cancel{2}x=-5 \end{array}$$

$$10.) |3x - 7| = 10$$

$$\begin{array}{l|l} 3x-7=10 & 3x-7=-10 \\ \hline +7 & +7 \\ 3x=17 & 3x=-3 \\ \hline \cancel{3}x=\frac{17}{3} & \cancel{3}x=\frac{-3}{3} \\ \hline x=\frac{17}{3} & x=-1 \end{array}$$

Examples

$$11.) |4x - 1| - 7 = 2$$

~~+7 +7~~

$$\begin{array}{l} |4x - 1| = 9 \\ \begin{array}{l} 4x - 1 = 9 \\ \cancel{+1} \quad \cancel{+1} \\ 4x = 10 \\ \cancel{\div 4} \quad \cancel{\div 4} \\ x = 2.5 \end{array} \quad \begin{array}{l} 4x - 1 = -9 \\ \cancel{+1} \quad \cancel{+1} \\ 4x = -8 \\ \cancel{\div 4} \quad \cancel{\div 4} \\ x = -2 \end{array} \end{array}$$

Classwork

- Pg 356 # 6-11

Homework

- Pg 356 # 19-39 odd